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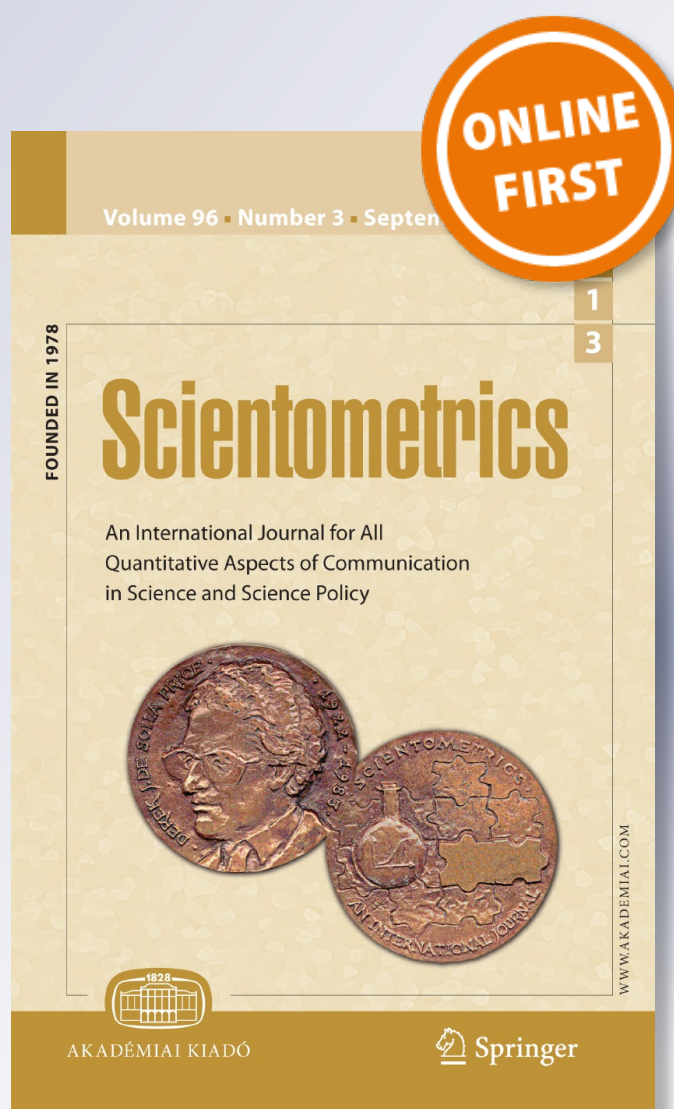
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Abstract Using an exhaustive database on academic publications in mathematics all over the world, we study the patterns of productivity by mathematicians over the period 1984–2006. We uncover some surprising facts, such as the weakness of age related decline in productivity and the relative symmetry of international movements, rejecting the presumption of a massive “brain drain” towards the US. We also analyze the determinants of success by top US departments. In conformity with recent studies in other fields, we find that selection effects are much stronger than local interaction effects: the best departments are most successful in hiring the most promising mathematicians, but not necessarily at stimulating positive externalities among them. Finally we analyze the impact of career choices by mathematicians: mobility almost always pays, but early specialization does not.

Keywords Faculty productivity · Organization of research · Peer effects in science

JEL Classification D85 · I23 · J24 · L31

We are grateful to *Mathematical Reviews*, published by the *American Mathematical Society*, for allowing us to use large data from their base to conduct the study presented here.

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Introduction

In spite of a growing interest about the determinants of success in academic research, very little is known about the cross-country and intertemporal patterns of productivity by researchers and universities. Most studies focus only on one country (typically the US) and very often look only at a small number of journals, a subset of universities and a limited time period. For example Laband and Tollison (2000) compare the patterns and impact of scientific collaboration in economics and biology, but they focus on the three top academic journals in each field and look only at US universities. Oyer (2006) looks at the impact of initial placement on the career of PhD economists but he only looks at the economists who graduated in seven US economics departments. Similarly, when Agrawal and Goldfarb (2008) look at the impact of Bitnet (an early version of Internet) on university research output in engineering, they only look at US universities on the period 1981–1991. Even if Kim et al. (2009) consider a longer time interval (1970–1999) in their study of the impact of new information technologies, they look only at US universities. As suggested by Coupé (2003), this might be due to a comprehensible “home bias” (“US economists rank US institutions,... Canadian economists restrict themselves to Canadian departments,..., Asian economists focus on Asian departments” Coupé (2003) p 1309) but lack of data must also play a role, and more precisely the difficulties that arise when trying to use worldwide data sets on academic research outputs.

There is an important exception to this lack of structured and easy to use data: the American Mathematical Society maintains an almost exhaustive database (*Mathematical Reviews*) of publications in mathematical journals all over the world. This unique database¹ provides a fantastic opportunity for studying the international and inter-temporal patterns of academic research.

Mathematics is an interesting field to study in terms of knowledge production. Indeed, this discipline is special in several ways: (1) there is relatively little equipment needed to do research, unlike biology, physics and engineering or even economics and psychology, (2) many papers are still written by single authors, partly defying the trend documented by Wuchty et al. (2007); Jones (2010), (3) language barriers are perhaps less important than in other fields, (4) (relatedly) elite mathematical research departments are relatively international, (5) math is less constrained by local interests than social sciences (i.e. Americans may care most about the US economy), the humanities (i.e. the French may disproportionately care about French literature), and even engineering (i.e. Australians may disproportionately care about geological engineering). Therefore, out of all fields, the underlying structure of knowledge production in mathematics suggests that local effects should be relatively unimportant. This means that, in addition to the availability of a rich dataset, mathematics is useful to study because many of the constraints associated with knowledge production are less binding than in other fields.

The quality of *Mathematical Reviews* data is apparent in several ways, two of which are of particular relevance here. The first is that it is almost exhaustive: it covers the worldwide mathematical production over the period studied here, 1984–2006. As explained below, we focus our attention on a subset of mathematicians and journals, but our sample is remarkably large: we are able to study the academic output of the 32574 mathematicians who were active all over the world over the period 1984–2006. Second, our data set is

¹ To our knowledge, Borjas and Doran (2012) are the only ones to use the same source of data. They study the effects of the collapse of the Soviet Union and the influx of Soviet mathematicians after 1992 on the productivity of their American counterparts.

unique because it is remarkably well structured and easy to use: each institution and each author can be identified without ambiguity, as well as the main and secondary fields of the articles. This allows to identify precisely all the career decisions made by mathematicians: choice of fields and co-authors, and more importantly mobility decisions. All movements of a researcher from one university (and one country) to another can be perfectly tracked down, at least for mathematicians who remain active (i.e. continue to publish), which is the focus of our interest in this article. We are thus able to identify international and inter-department movements of mathematicians at the aggregate level and also to assess the impact of these movements on the individual productivity of researchers. Given that at least some proportion of this mobility is due to exogenous reasons (other than offers made to the best mathematicians by the most prestigious institutions), we can estimate the impact of mobility on the future productivity of researchers. For the same reason, we can assess the impact of career decisions (specialize or not, collaborate or not,...) on the success of a mathematician. Even though mathematics clearly has its own specificities (we will come back to these specificities later), we are convinced that our study can also be useful for understanding the determinants of academic success in other fields.

The first part of the article provides detailed descriptive statistics on academic production by mathematicians and uncovers some surprising facts. For example, contrary to a widely held belief (among both scientists and lay people) the rate and quality of mathematical production does not decline rapidly with age. For mathematicians who remain scientifically active, productivity typically increases over the first 10 years, then remains almost constant until the end of their career. However, there is a substantial attrition rate (i.e. mathematicians who stop publishing) at all ages.² Another surprising fact is how fast the shares of mathematical production by different countries have changed in the recent years. The US is still by far the largest country in terms of mathematical production, but their share has declined from 50 % in 1984 to 34 % in 2006. While this phenomenon has been documented elsewhere (see e.g. Hill et al. (2007)) the magnitude of the US decline in mathematics is striking. It contrasts with other areas of science and engineering, where the share of the US in world scientific production was found to decrease much more slowly.³ Similarly, the share of China in mathematics is rapidly increasing but it is still surprisingly low as measured by our indicators, which put a strong weight on the most selective journals (only 3.8 % in 2006). Another surprising fact is that international mobility after the PhD is rather weak and it is much more symmetric than could be expected, both in terms of numbers of mathematicians and in terms of “quality”, as measured by the output of the mathematicians who change countries.

In the second part of the article we perform a detailed statistical analysis of the factors that can influence the scientific production of academic mathematicians. This allows to analyze the determinants of individual productivity all along a mathematician's career, taking into account the (unobserved) intrinsic “talent” of each mathematician through fixed effects. Location is of course among the important factors: the best mathematicians are (by definition) in the best departments, but causality is not clear. Using the mobility of a sizable subset of these mathematicians [as in Kim et al. (2009)] we can separate the selection effects (hiring the most promising mathematicians) from interaction effects

² For comparable studies in other fields see Levin and Stephan (1991) and Stephan (2008).

³ This is consistent with Annex Table 3 in Hill et al. (2007), where mathematics appears as an area where the US share of world output has decreased the most from 1988 to 2003. Our data show a continuation of this trend up to 2006.

(stimulating positive spill-overs through exchange of expertise and feedback among colleagues).

In conformity with other recent studies [e.g. Waldinger (2012)], we find that university fixed effects (once researchers intrinsic quality is accounted for) are in general small, and are not strongly correlated with the quality of the department. A few departments have a strong positive impact on their members' productivity but in prominent examples this is largely associated with prestigious locally managed journals, which seem to publish relatively many articles from "locals".

We also analyze the impact of other characteristics of departments on the outputs of their members and find several interesting facts. First, we find that size does matter: large departments are good for individual productivity. However this effect is largely due to good hirings and becomes negligible when authors fixed effects are incorporated. Then, it appears that having a specialized department has a negative impact on productivity when no fixed effect is used, but this impact becomes positive with fixed effects. This tends to indicate that a narrower scope lowers the quality of hiring, but that researchers fare better in a department with colleagues close to their mathematical interests. Looking at US universities, we find several interesting results. First, money does not seem to matter much: even though the endowment per student has a strong positive impact when authors fixed effects are not used, it has a *negative* impact (although not very significant) when these fixed effects are incorporated. This negative effect becomes more significant when taking into account whether the university is public or private. Second, the fact that a US university is private has a small positive effect compared to public ones. There is also a sizable positive effect of location on the East Coast relative to the Mid-West, the West Coast standing in between the two.

Finally we analyze the impact of career decisions of individual researchers. We obtain some additional interesting results on collaborations, mobility and specialization. Collaborations have a globally negative effect: the total output of mathematicians who have more collaborating authors tends to be lower than the output of those who work separately. However, the impact of collaborating with authors of a different specialty is positive: interdisciplinary work (within mathematics) spurs productivity. Concerning mobility, we find that each move increases future production. Regarding specialization, we provide evidence that a high level of specialization is not a good strategy: it is correlated with a *lower* future output, in particular for young researchers. This suggests that researchers should be encouraged, especially at a younger age, to keep a broad range of interests.

The remainder of the paper is organized as follows. "[Data description](#)" section presents the data. "[Descriptive statistics](#)" section gives some descriptive statistics (on the data). "[Analysis of the scientific output of mathematicians](#)" section analyzes the determinants of scientific output of mathematicians. "[Conclusion](#)" section concludes.

Data description

The *Mathematical Reviews* database

The data come from the Mathematical Reviews database, which is maintained by the American Mathematical Society. This database provides an almost exhaustive source of information on publications in mathematics, covering almost all journals publishing mathematics-related articles and many books and conference proceedings. It is remarkably well structured and has three features that make it particularly well suited for statistical use.

First, it provides a personal identification of each individual author, so that there is no ambiguity even when two authors have the same name and initials. Second, each institution is identified by a unique institution code. Last, each article is assigned one or more codes describing its principal and secondary fields within mathematics using the “mathematical sciences classification (*M.S.C.*)”. This gives a precise description of an article’s area within mathematics.

A small portion of the *Mathematical Reviews* database was used: since our focus was on “active” mathematicians, we selected the 98 journals with the highest impact factor among those with a cited half-life above a threshold (according to the 2006 *Journal Citation Report* in pure and applied mathematics), and compiled a list of all 129,242 articles published in those journals between 1984 and 2006. Those 98 journals are the most visible in fields of pure and applied mathematics, so that our data paints a reasonably accurate picture of the best part of mathematical research. The precise number of journals considered here—98—is somewhat arbitrary and follows from the threshold applied for the selection of the list of journals. However, the list is large enough to covers most mathematics articles considered as important in their subfield. Moreover the choice of weights attributed to journals (see below) is such that lower-impact journals have a much smaller weight in the statistical analysis, so considering a longer list of journals would presumably not change most of the results obtained below. We chose 1984 as the starting date because *Mathematical Review* only records the affiliation of authors from this date.

We then compiled a list of all 32,574 mathematicians who published at least two articles in those 98 journals over this period. For these mathematicians, we compiled a list of the dates of their first and last publications in the whole database (not just the 98 journals in our restricted list). We focused mainly, but not exclusively, on this smaller group of “active” mathematicians. The others, those with only one article in our list of 98 journals, can be of different types: mathematicians publishing few papers, mathematics PhD who have left the field, or academics of another field who have collaborated to a project published in a mathematics journal, etc.

Impact

For a correct assessment of the activity of the mathematicians in our list, we did not use the most standard impact factor data, which covers all scientific areas but is of limited relevance for mathematics [Adler et al. (2009)]. Instead, the impact of each journal in the mathematical community was evaluated by its 2007 *Mathematical Citation Quotient* (*MCQ*), which is a kind of impact factor computed over five years by *Mathematical Reviews* using their data. It is defined for each journal as the mean number of citations of its articles, within 5 years of publication, in a relevant part of the mathematical literature. This *MCQ* is highly correlated with the *Impact Factor* (*IF*) as computed by Thomson Reuters, but it is less volatile and appears to be much more relevant for mathematical journals for at least two reasons. One is that the 5-year window considered for the *MCQ* is more significant than the 2-year window used for the impact factor, which is important for mathematics where articles typically attract citations slowly and over a long period of time (especially in some subfields, like number theory). The other is that the citations are counted over a well-chosen and significant part of the mathematical literature, while the *IF* is computed over a choice of journals which, in the area of mathematics, is more arbitrary (for instance some relatively important journals are excluded). Those two differences mean that the *IF* tends to generate larger biases than the *MCQ* between subfields of mathematics. Note however, that our statistical treatment is designed to limit those biases.

However the *MCQ* is only an indication of the “quality” of a journal as evaluated by most mathematicians, rather than an absolute measure. In order to have a reasonable assessment of the importance of an article, we decided to assign to each article a weight equal to the product of its number of pages by the *square* of the *MCQ* of the journal where it was published. In this way, longer articles have a (linearly) higher weight. This is chosen in view of the general practice in mathematics: selective journals tend to be more demanding towards long papers, and to accept more easily short notes. Not taking into account the length of papers would give higher weight to authors who split their output in many short contributions compared to those who prefer to make fewer, more important papers. This would therefore bias the results. The square is justified by the desire to emphasize good quality journals. Doing so, the weight of a page varies within our limited list of journals in a ratio of approximately 1 to 100. Putting a much stronger weight on a small number of highly selective journals, as we do by taking the square of the *MCQ*, also reflects the confidence most mathematicians still have in the quality of peer review in the most selective journals. This might not be the case in other areas, see for instance Ellison (2011) for questions on the value attached to publications in top journals in economics, or Ellison (2012) for an analysis of the (quite different) situation in computer science.

Our choice of weights puts a strong emphasis on a small number of very selective journals, as can be seen from the list of journals in the appendix. This selectivity is in conformity with the most widely shared quality assessments within the community of mathematicians. However, we have checked that choosing a different weight on articles does not change significantly the results of our study. There are probably some biases in the way different fields are treated (for instance journals in applied mathematics tend to have a lower *MCQ* than those in pure mathematics), but this is controlled for in our regressions by using the field of research as a control variable.

A key point, however, is that the main results obtained here do not depend on the precise indicator used. We give in Appendix 2 some results duplicating those presented in the paper with different quality measures, replacing in particular the *MCQ* by the more familiar *Impact Factor (IF)*, which is more commonly used in natural sciences but seems less well adapted to mathematics. In this appendix, the weight of each paper is the product of its length (number of pages) by the mere *IF* of the journal where it is published (as opposed to its square that we use in our other regressions). As the reader can check, our main results do not change much if we adopt these quite different measures of output. Smaller changes—like suppressing the square on the *MCQ*—have an even smaller impact on the results.

To achieve a better understanding of these differences between fields within mathematics, we used the *Mathematical Subject Classification (M.S.C.)* codes assigned to each article by *Mathematical Reviews*. Since this classification is quite detailed, we grouped different *M.S.C.* codes so as to obtain only 10 different areas. There are sizable differences between the characteristics of articles in different fields of mathematics, as seen in Table 12 in the Appendix 1. We also indicate in this table the number of authors and of articles for each field, so as to give an idea of their relative numerical importance. It shows simply that Probability and Statistics is the largest field while Analysis is second followed by Partial Differential Equations, Differential Geometry, Numeric Methods and Physics. Topology and Algebra come after and the smallest field is Dynamical Systems.

Finally, we compute a yearly “author impact”, defined for each author and year as the sum, over all articles published by this author in a given year, of the weight of each article divided by the number of authors. In this way, the “output” corresponding to an article with multiple authors is shared between them (equally).

Any method for attributing “weights” to scientific articles and thus to researchers’ outputs has necessarily some degree of arbitrariness. There is a growing literature trying to determine the best way to measure scientific output. For instance, Hirsch (2005) proposes to measure the productivity of authors by the so-called h-index. This index is criticized by Ellison (2010). Palacios-Huerta and Volij (2004) propose a new index based on citations but different from the traditional Impact Factor. Combes and Linnemer (2003) propose a ranking of journals in economics based on peer assessment of journal quality in addition to citations instead of a purely objective measure using citation counts. Consistently with Korevaar (1996), we believe that our way of weighting articles gives a result that is not too far from the heuristic assessment of many mathematicians, but we have not, at this point, tried to make this precise. It is probably *not* well adapted to other scientific areas.

Descriptive statistics

This section contains general data on the spread of mathematical research (as measured by our indicators) in the world, on collaborations between regions and on mathematicians moving from one country to another. We also consider evolutions over time. Location of mathematicians can be identified thanks to their university affiliation as recorded in publications. The list of coauthors and their affiliations as well as the evolution over time of affiliations for a given author allowed us to identify international collaborations as well as movements of mathematicians.

Countries and regions

The weight of different regions over time

In the following results, we present statistics for the ten countries having the biggest mathematical production, which are, by alphabetical order, Canada (CA), France (FR), Germany (GER), Israel (IL), Italy (IT), Japan (JAP), the People’s Republic of China (PRC), Spain (SP), Britain (UK), and the United States (US). Russia (including the former U.S.S.R. before 1989) does not appear among them because most Russian mathematicians were publishing for a long time in domestic journals in Russian that had consequently low impact factors because rarely read by the international community.

Table 1 shows the proportion of world output coming from different countries, over time. Two striking features are the decrease in the share of the US and the increase in the share of China, which however remains quite low.

Collaborations

As shown by Table 13 in the Appendix 1, the evolution over time of the proportion of international collaborations is particularly impressive for Russia. Before the fall of the Soviet Union in 1989, it was difficult for Russian mathematicians to collaborate with foreign colleagues. After 1989, a large proportion of the most active Russian mathematicians moved to other countries, which can account for the high proportion of collaborations between mathematicians located in Russia and those in other countries.

Note that the proportion of collaborations in the US was initially quite low (25 %) but is has increased markedly over the period.

Table 1 Share of countries in the world production, over time (in percentage points)

Years	Country										
	CA	FR	GER	IL	IT	JAP	PRC	SP	UK	US	OTH
1984–1986	2.1	10.4	6.5	1.2	1.7	3.4	0.2	0.8	4.0	50.9	11.9
1987–1990	2.8	10.6	5.9	1.4	2.3	3.2	0.7	1.0	4.0	50.6	13.3
1991–1994	3.6	11.0	6.0	2.1	2.6	3.7	0.9	1.2	3.7	49.8	11.5
1995–1998	3.7	11.3	7.2	2.3	3.1	3.6	1.3	1.6	4.4	44.2	12.9
1999–2002	2.6	12.5	6.8	3.0	3.2	3.6	2.6	2.1	4.8	38.9	13.0
2003–2006	3.2	12.6	6.3	1.8	3.9	3.9	3.1	2.5	4.6	36.3	13.3

Table 2 Mean impact of mathematicians with first location in/out of the country of their current location

Origin	Country											Total
	CA	FR	GER	IL	IT	PRC	RUS	SP	UK	US		
Locals	4.9	12.4	8.2	8.9	5.6	4.1	6.3	4.7	6.6	8.9	8.0	
Migrants	11.9	17.3	13.1	10.4	11.8	8.9	8.5	11.3	12.2	13.3	10.4	
Average	7.7	13.1	8.9	9.3	6.6	5.1	6.4	5.3	8.1	9.4	8.5	

International mobility

Table 14 in the Appendix 1 shows the percentage of total number of years spent in different countries by active mathematicians with a known first location in a given country. The total in each row is the total number of years for which an affiliation is known for any of the mathematicians in our database with first affiliation in the corresponding country, and the total in each column is the total number of years spent in each country by mathematicians with a known affiliation.

Table 14 contains a precise indication of the gain/loss of each country from the “brain-drain”, seen by comparing the total on a column (number of years spent in a country by active mathematicians) to the total on the corresponding row (number of years spent by active mathematicians with first career affiliation in the country). For instance the US benefit from the flow (25,921 years spent by active mathematicians in the US, versus 22,882 years spent anywhere by mathematicians with location in the US) while Russia loses (210 vs. 330 years).

The variable “first location” is defined as follows. We know the affiliation of mathematicians for each year in which they have published a paper in one of the journals in our list. However we also have, for each mathematician in our list, the date of their first publication (in any journal, not necessarily those in our list). We define the “first location” with the first affiliation that we know of, *if* it is within 3 years of the first publication. As a consequence we know the first location of only 10,803 of the 32,437 “active” mathematicians in our database. In particular we do not know the “first location” of any mathematician with first publication before 1981, since our list of articles starts in 1984.

Table 3 Proportion of mathematicians residing in one country and “coming from” (having had their first publication in) another country

Country	Proportion
Canada	0.39
France	0.15
Germany	0.15
Israel	0.29
Italy	0.16
Japan	0.05
China	0.20
Spain	0.10
UK	0.26
US	0.12

In general, this “first location” indicates the country where mathematicians have completed their PhD, or the country of their first or second year of post-doc. We only consider here mathematicians for whom we know the affiliation of first publication.

A striking feature of Table 14 is the relatively small number of mathematicians who have changed countries: the vast majority remains in the country of their first location. The only exception is the high number of moves between Canada and the US, in both directions. However, as mentioned above, the sums of the rows and columns corresponding to each country indicate the gain/loss from the flows, which are close to 10 % for countries like the UK (loss) or the US (gain).

Table 15 in the Appendix 1 gives a hint on the attractivity of different regions. It shows the mean impact of mathematicians working in a given region, depending on the region where they had their first publication, which is typically the region where they did their PhDs. Therefore these results must be interpreted with caution, given that apparent “migrations” may correspond to an authentic “brain drain” but also to a mere return to the country of birth. A second reason for caution is that the numbers involved (e.g., migrations from Germany to Japan) maybe quite small.

Table 2 has an interesting implication: in almost all regions, the mathematicians having their first location outside their current region (“migrants”) have a better mean impact than those with a local first location (“locals”). Here again the explanation can vary between countries; in some cases it can be that the most active scientists tend to be those who went abroad to do their PhD before coming back, while some other countries actually drain the most active scientists.⁴

The proportion of “migrants”, i.e. mathematicians having their first location in a different region than their current location, is shown in Table 3. These proportions are an indication of how attractive a country is for foreign mathematicians, and of how open its institutions are to mathematicians with a foreign PhD. Canada strikes out as particularly open. The relatively high figure for China is certainly a measure of the number of mathematicians returning to China after a PhD, and therefore a first publication, in another country. The small number for the US is also due to the fact that a lot of migration towards the US is done before and not after the PhD.

⁴ The data in Table 15 and in Table 2 is more or less significant depending on the countries, as indicated in the numbers of mathematicians concerned, as seen in Table 14 in Appendix 1 and in Table 3.

Table 4 Percentage shares of the world output over time, top 20 departments

University	Rank	Share of impact	1984–1988	1989–1994	1995–2000	2001–2006
Princeton	1	1.80	2.15	1.96	1.61	1.70
Paris 11 (FR)	2	1.73	1.73	2.25	1.56	1.50
MIT	3	1.58	1.94	1.94	1.44	1.30
NYU	4	1.44	1.63	2.05	1.49	0.89
Berkeley	5	1.39	1.80	1.44	1.34	1.21
Harvard	6	1.27	1.94	1.18	1.38	0.94
Paris 6 (FR)	7	1.27	1.27	1.26	1.42	1.14
Chicago	8	1.09	1.23	1.06	1.07	1.08
UCLA	9	0.97	1.26	1.30	0.75	0.79
Stanford	10	0.93	0.99	1.16	0.83	0.84
Michigan	11	0.93	0.64	0.90	1.18	0.85
Rutgers	12	0.92	1.09	1.08	1.04	0.63
Purdue	13	0.91	1.53	1.08	0.75	0.64
Minnesota	14	0.86	0.87	1.24	0.68	0.75
Maryland	15	0.85	1.26	1.06	0.84	0.53
IAS Princeton	16	0.79	0.89	0.82	0.89	0.63
Toronto	17	0.77	0.46	0.88	0.82	0.79
Ohio State	18	0.75	0.75	0.80	0.82	0.63
Columbia	19	0.72	1.15	0.83	0.62	0.54
Wisconsin	20	0.71	0.91	0.68	0.56	0.77

We have not included Russia in this table because, as mentioned above, its researchers could not publish before 1989 in the journals of our list. As a consequence we cannot reliably identify their first affiliation, which skews the results for this country.

Up to this point we have only considered the relationship between the first location of mathematicians and their locations when they publish new articles. We now concentrate on “permanent” moves between regions, defined as follows: mathematicians who have spent at least 3 years in a given region, then moved to another region and spent at least 3 years there. This excludes short moves for short-term post-doctoral positions or sabbaticals, but also changes of country immediately following the first publication. Tables 16 and 17 in the Appendix 1 show these modified “migration” data and illustrate three striking facts. First, the number of such “permanent” moves between countries is small (see Table 16). Second, the numbers of “permanent” moves between most couples of countries are remarkably symmetric. Third, the “quality” of those moves, as measured by the mean impact of the mathematicians moving between countries, is also remarkably symmetric as shown in Table 17 in the Appendix 1. Our data tends to indicate that the “brain-drain” phenomenon happens mostly for young researchers who move before or after their PhD or after a few years of post-doc. Incidentally, this finding suggests that investing a lot in PhD programs attended in large part by foreigners, like the US does, might turn out to be a very good idea, given the fact that a large proportion of these foreign students does not return to their country of origin.

Table 5 Rank for total output versus rank for mean output

Rank	University	Total impact	Rank by mean	Mean impact
1	Princeton	42,522	3	25.7
2	Paris 11 (FR)	40,800	6	20.1
3	MIT	37,408	13	16.1
4	NYU	34,136	7	19.3
5	Berkeley	32,770	27	12.0
6	Harvard	30,002	4	25.0
7	Paris 6 (FR)	29,931	36	11.4
8	Chicago	25,875	8	17.8
9	UCLA	22,835	23	13.4
10	Stanford	22,074	31	11.7
11	Michigan	21,931	51	10.1
12	Rutgers	21,724	40	11.1
13	Purdue	21,477	29	11.9
14	Minnesota	20,387	57	9.4
15	Maryland	20,122	39	11.2
16	IAS Princeton	18,592	2	33.2
17	Toronto	18,157	33	11.6
18	Ohio State	17,625	42	10.8
19	Columbia	16,987	14	15.8
20	Wisconsin	16,755	62	8.9

Universities

General description

Table 4 shows the share of world output (measured by our indicator) for the top 20 departments (also ranked by this indicator), and its variation over time. It shows notable changes in the ranking of departments, both upwards and downwards. Another feature is that the production of mathematical literature, even when measured by our quite elitist indicator, is not very concentrated. Indeed, the department ranked first produces only 1.8 % of the world total output (weighted by impact) over the whole period. Moreover this concentration appears to decrease over time, since the share of the most active department was 2.25 % in 1989–1994, but only 1.7 % in 2001–2006.

Table 18 in the Appendix 1 shows the size (yearly average number of active mathematicians) and the share, in total output, of the top author, and then the top 5 and top 10 authors (again weighted by impact). The share of the most productive author typically varies between 5 and 15 %, while the share of the top 10 authors varies between 23 and 70 %, depending on the size of the department.

Table 5 shows the top 20 departments by total output, ranked now in terms of the average output of their researchers (among departments with a total output of at least 5,000 weighted pages over the period, so as to eliminate very small departments). There is a large difference between the two rankings, since small departments with highly productive researchers (like the Institute for Advanced Studies) have excellent rankings in terms of average output but not in terms of total output. The top department by mean output is the

Table 6 Share of total number of years spent by very active (resp. active, resp. young) mathematicians (mean over period of study)

University	Rank	Size	Share top 100	Share top 500	Share young
Princeton	1	96.9	8.73	3.82	0.76
Paris 11 (FR)	2	105.5	4.23	3.21	0.64
MIT	3	123.2	3.04	2.59	0.96
NYU	4	102.5	4.83	2.34	0.61
Berkeley	5	146	2.11	2.56	0.9
Harvard	6	64.9	5.04	2.85	0.55
Paris 6 (FR)	7	143.1	2.01	1.51	0.77
Chicago	8	81.1	2.22	2.43	0.62
UCLA	9	93.8	3.36	1.24	0.47
Stanford	10	106.7	2.11	1.9	0.7
Michigan	11	111.8	0.11	1.74	0.69
Rutgers	12	104.2	2.01	1.74	0.39
Purdue	13	95.5	2.44	1.59	0.45
Minnesota	14	116.5	0.22	0.92	0.73
Maryland	15	95.6	2.49	1.65	0.37
IAS Princeton	16	33.2	2.39	1.28	0.22
Toronto	17	78.7	1.19	1.4	0.44
Ohio State	18	86	1.36	0.86	0.43
Columbia	19	57.2	2.49	1.42	0.38
Wisconsin	20	101.3	0.11	1.17	0.5

I.H.E.S. (Institut des Hautes Etudes Scientifiques, Paris) , but it does not appear in the table since it is not part of the top 20 departments by total output.

Where are the most active mathematicians?

Table 6 shows the ranking of the 30 top departments by total output, along with their size (mean number of active authors) and average share (%) over the period of the top 100 authors by total output, and the share of those among the top 500 by total output. The table shows relatively little concentration of the mathematicians with the highest output in the top departments, indicating again the relatively high number of departments taking part in top-level research. The last column shows the share of young mathematicians (those at most 4 years after their first publication), it gives an indication of the concentration of future active mathematicians (those which end up in our list) in the departments, and therefore of the importance of departments as a breeding ground for future mathematicians.

Analysis of the scientific output of mathematicians

We now undertake a more elaborate analysis of the determinants of scientific “productivity” for mathematicians.

For such an analysis, we postulate that the output measure of mathematician *i* during period *t*, denoted *y_{it}*, follows a linear model :

$$y_{it} = \alpha_i + \theta_{u(i,t)} + \gamma_{f(i,t)} + \delta_t + \beta X_{it} + \varepsilon_{it} \tag{1}$$

Table 7 Effect of individual variables on mathematician's output

Dependent variable	(1)	(2)	(3)	(4)	(5)
Author Impact	OLS	OLS	OLS	2SLS	2SLS
Explanatory variables					
Nb. of coauthors	-1.598*** (0.0705)	-1.224*** (0.0749)	-2.858*** (0.0957)	-4.653*** (0.778)	-3.930*** (0.633)
Nb. coauthors diff specialty	2.768*** (0.307)	2.387*** (0.252)	1.741*** (0.272)	2.399*** (0.337)	5.090** (2.449)
Nb. past moves	1.595*** (0.0675)	0.888*** (0.0597)	1.233*** (0.153)	1.259*** (0.121)	1.280*** (0.117)
Nb. of past author's fields	-0.483*** (0.108)	0.303*** (0.113)	-0.642*** (0.210)	-1.040*** (0.187)	-0.895*** (0.185)
Nb. of past sub-fields (<i>M.S.C.</i> codes)	1.579*** (0.144)	1.084*** (0.108)	1.301*** (0.173)	1.527*** (0.127)	1.342*** (0.125)
Nb. of past coauthors	-0.0212 (0.0339)	-0.159*** (0.0311)	-0.238*** (0.0431)	-0.125** (0.0610)	-0.218*** (0.0556)
Author fixed effects	No	Yes	Yes	Yes	Yes
Year fixed effects	Yes	Yes	Yes	Yes	Yes
Field fixed effects	Yes	Yes	Yes	Yes	Yes
University fixed effects	No	No	Yes	Yes	Yes
R^2	0.140	0.099	0.118		
Observations	551,655	551,655	296,538	260,007	268,892
Number of authors	60,560	60,560	54,183	29,388	29,669

where $u(i, t)$ is the university of author i at year t , $f(i, t)$ is the field of research of author i at year t , δ_t is a period effect, X_{it} are time varying characteristics of author i (for example, age, age squared, age cubed and number of coauthors) and α_i is a fixed effect for author i capturing the effect of all unobserved characteristics of the author (fixed over time) that affect his or her productivity. Assuming that ε_{it} is mean independent of $\alpha_i, \theta_{u(i,t)}, \gamma_{f(i,t)}, \delta_t, X_{it}$, we can identify all parameters using Ordinary Least Squares (OLS). For inference, we use clustered standard errors at the level of each author.

A causality interpretation can be done, provided all right hand side variables in this equation are exogenous. This means that the unobserved heterogeneity of authors that is correlated with productivity and with some of the right hand side variables (like the university or the number of coauthors) is fixed over time. This assumption would be invalid if, for example, universities would hire mathematicians based on temporary and unobserved shocks of productivity, therefore correlated with ε_{it} .

Our first strategy is based on the use of author fixed effects to account for the endogeneity of placement of mathematicians in departments. As no experimental framework is possible in this area and we cannot really justify any natural experiment that would allocate researchers randomly to academic departments, we believe that fixed effects is a good strategy in such a reduced form estimation. In order to account for the possible correlation between unobserved university quality and moving decisions, we also estimate a specification where we add university fixed effects in $\theta_{u(i,t)}$. An alternative strategy, consisting in estimating a fully structural model of hiring and moving decisions, is beyond the scope of this paper. However, moving from one department to another is a costly decision that is not likely to be subject to unexpected and temporary shocks in performance of authors such

that the correlation between performance and placement of authors is more likely to be due to the long term performance level of researchers, something captured by the author fixed effect in our specification. We thus consider that this fixed effect strategy is quite powerful in controlling for the endogeneity of the department where mathematicians are enrolled. The only sort of endogeneity that our empirical strategy cannot account for is when both unobserved deviations from its mean of university quality and author productivity shocks are correlated. This simultaneity bias would prevent us to identify the causal effect of university characteristics on author performance but we do not believe that it is likely to be an important problem. We will have to keep this caveat in mind when interpreting results though.

With this specification, $\theta_{u(i,t)}$ can be interpreted as the effect of the university or department on the output of individual i . This effect can be identified because mathematicians move from departments to departments and thus $u(i, t)$ is not fixed over time. Therefore θ_u identifies the average effect of university u on mathematicians who have been affiliated to that university in year t : by definition of the indicator $u(i, t)$, they are such that $u(i, t) = u$. Similarly $\gamma_{f(i,t)}$ can be identified because not all authors publish always in the same field and thus variations at the individual level of fields of publication allow the identification of “field effects” in addition to individual effects. One alternative model consists of assuming that there is no unobserved heterogeneity across authors and thus that $\alpha_i = \alpha$ for all i or that the deviations from the mean α_i are mean independent of all other right hand side variables of the previous equation. Then, one can add time invariant variables in the X_{it} and still identify their effect.

We estimate several variants of the specification of Eq. (1) and first start with the analysis of the determinants of individuals' performance in terms of author impact. Then, we consider in more detail the effect of departments qualities on researchers, then the effect of specific characteristics of departments. Finally, we focus on results for US departments and provide more detailed evidence on the life-cycle of authors performances.

Determinants of Individuals' Impacts

We estimate Eq. (1) with several individual characteristics as explanatory variables X_{it} . These explanatory variables are the number of co-authors, and the current number of co-authors from different fields, some variables on authors' personal histories like the total number of past co-authors, the number of subfields (or mathematical subject classifications (*M.S.C.* code)) in which they have published, and the number of institutions where they have held a position. More precisely, we have defined the number of co-authors (at a given time period) as simply the number of total coauthors who co-signed a publication with the author (co-authorship with the same coauthor for several publications in a year is infrequent but counted). We also determine the main specialty of each author by the most frequent *M.S.C.* code among his or her publications and define field fixed effects according to this specialty. This also allows us to measure a second indicator of collaborations, namely the number of co-authors having a different specialty. The number of past moves between two departments is the number of times that the author has changed location since his first publication (recall that changes of location are identified only when the author publishes). The number of past *M.S.C.* codes of each author is the number of sub-fields measured by *M.S.C.* codes of his articles in his past publication records and the number of past co-authors is measured simply by compiling the list of all distinct co-authors from the list of past articles published that are co-authored.

Column (1) of Table 7 estimates Eq. (1) by OLS with the author impact as dependent variable but without author or university fixed effects⁵. In column (2), we add author fixed effects as unobserved heterogeneity on authors research quality may be correlated with several right hand side variables and bias the coefficients estimates. Then, in column (3), we also add university fixed effects because unobserved university specific effects may affect the performance of researchers and be correlated with their co-authorship and other right hand side variables. Remark that the sample size drops when we have both author and university fixed effects, mostly because we need both authors moving universities and varying right hand side variables in order to identify those coefficients. Finally, in columns (4) and then (5) we keep the author and university fixed effects but also instrument first the number of coauthors (in column (4)) and then both the number of coauthors and the number of coauthors in different specialties [in column (5)] with the same variables lagged twice in order to avoid some simultaneity bias in the change in the number of coauthor and the change in the author impact.

A remarkable finding in Table 7 is that the current number of co-authors has a negative impact,⁶ with or without author fixed effects, but also with university fixed effects or when we account for some possible simultaneity bias by instrumenting the number of coauthors by its lagged value. This suggests that generally speaking, collaboration does not spur productivity: the output of a group of researchers, measured in terms of weighted pages published, is lower than it would have been if each of them had worked separately. Moreover, the comparison of coefficient estimates in column (3) and (4) shows that instrumenting the number of coauthors reduces the absolute value of the negative effect on author impact, showing that time varying unobserved factors increasing author impact are negatively correlated with the current number of coauthors.

However, the number of past co-authors with different specialties has a positive impact. This is true independently of whether we account for unobserved author and university fixed effects. Moreover, the number of co-authors from different fields also has a positive impact when instrumented by its lagged value [column (5) of Table (7)]. One interpretation is that collaboration with colleagues with a closely related competence is detrimental to total impact per author, but collaborating with mathematicians from a different main field is useful. It is remarkable that the coefficient of the number of coauthors from different fields more than doubles when it is instrumented by its lagged value. It shows that the simultaneity of author impact and the number of coauthors from different specialties is present. Actually, the unobserved time varying factors that increase the author impact are negatively correlated with the number of coauthors from different fields. Having published in the past in different fields or in different sub-subfields has opposite effects (except when we include author fixed effects but no university fixed effects). However, the overall effect is positive, meaning that the variety of sub-fields of publications in mathematics has a positive effect provided it stays within an identified field of mathematics. The number of past institutions is also clearly positive [coefficient of the number of past moves in Table (7)], which is consistent with our previous observations on the number of past subfields and of past co-authors: having been exposed to a wider spectrum of mathematical ideas has a positive effect on mathematical output.

⁵ In all tables, *** means that the coefficient estimate is significantly different from zero at 1 percent level, ** at 5 percent and * at 10 percent.

⁶ Recall that in our individual output measure, the impact of each paper is shared between the authors.

Effects of departments on individuals

Then, an interesting question is the impact of location on mathematicians' output: how important are departments for the scientific productivity of their researchers? In order to study this question, we look into more details at the estimated values of the university fixed effects estimated before but not shown. Again, we use the data on the yearly production of authors as dependent variable. The coefficients of department dummies reflect the average output of researchers belonging to those departments over the 1984–2006 period. As authors are moving across departments, we can also control for author fixed effects and separate the effect of the department itself from the average quality of the mathematicians composing this department.

Table 8 shows the estimated mean effect of the 30 main mathematics departments (in terms of total output on the period) on their researchers using regressions of author impact on department dummies without author fixed effects (in column 1) and then with author fixed effects in columns 2–4. Normalizing the constant so that the sum of the mean effect of the 30 departments under consideration is zero, the university effects just measure the “quality” of the department. When introducing author fixed effects, column 2 is for the whole sample period, while column 3 corresponds to the first period 1984–1994 and column 4 to the second period 1995–2006, in order to study the possible time variation in those effects.

Note that this analysis of the effect of departments on individuals, with fixed effects of the authors, is possible because there are many moves between departments. On average, each “active” mathematician in our base had 1.87 different locations over his lifetime, although this varies largely between countries.

Table 8 suggests that, generally speaking, the competitive advantage of elite mathematical departments does not seem to decrease between the first (before 1994) and the second part (after 1995) of our sample period. This contrasts with the findings of Kim et al. (2009) for economists [see also Agrawal and Goldfarb (2008)].

Table 8 also suggests that some elite departments have indeed a strong positive impact on their researchers. For instance being at N.Y.U. has a strong (although not significant) positive effect (13.17 weighted pages/year). However this effect becomes *negative* when the journal published by N.Y.U. (Communications in Pure and Applied Mathematics or CPAM) is taken out of the publications sample as shown in column 2 of Table 9.

The effect of local journals is also significant, albeit with a much smaller magnitude, for Paris 11 (its fixed effect falls from 22.98 to 16.32 when the geographically closest journal, *Publications Mathématiques de l'I.H.E.S.*, is not considered). This does not necessarily mean that referees and editors are more friendly to local authors, but might possibly be explained simply by the fact that these authors are encouraged to publish in the local journal.

Note that removing a journal also has an effect on the fixed effect of departments with no obvious relation to the journal. This can be explained by the fact that being in a given department encourages mathematicians to submit their paper to some journals more than to others.

Characteristics of departments

We now consider more specifically the effect of different variables characterizing the 30 most important departments.

Table 10 shows the influence of different variables on authors' impact and number of articles published after controlling for author fixed effects. The *University specialization*

index is defined as the sum of the squares of the proportions of the scientific output of the department in each field. It varies between 0 and 1, and is close to 1 for highly specialized departments and small for general ones. It is defined based on the subfield (*M.S.C.*, for Mathematics Subject Classification, as determined by *Mathematical Reviews*). The “Stability” variable is defined as the proportion of their total active life that mathematicians at a given department will spend there, so that it would be 1 for a department where everybody spends his whole active life, from first to last publication. It is an (inverse) indicator of mobility.

The first and second columns show the effect of the variables on the “impact” of authors taking into account the fixed effects of authors, with (column 2) and without (column 1) taking into account the fixed effect of the institution. Columns 3 and 4 are similar but measure productivity by the number of pages published instead of the impact. The coefficient of the variable “Stability” is not significant. The coefficient of the department size is positive and significant: bigger departments attract better researchers even after controlling for author fixed effects. The coefficient of the *University specialization index* is strongly positive on the impact of researchers, but not on the number of articles published: specialized departments appear to stimulate the quality of the production of their researchers, rather than the number of papers they write.

US departments

Table 11 shows the influence of some variables that are specific to the US: private vs. public universities, East Coast or West Coast, endowment per student. It also introduces a variable defined as *Closeness* which measures how “open” departments are, it is the mean of the proportion of its members “scientific life” that they will spend in this department.

The effect of the endowment per student is remarkable. It is strongly positive without authors fixed effects, meaning that rich universities can attract better researchers. However it is negative (but not significantly) when authors fixed effects are taken into account. This is rather counter-intuitive since a higher endowment could imply lower teaching loads and therefore more time for research. A possible explanation is simply that, once researchers have obtained a position in a well-endowed university, they have weaker incentives to publish first-rate articles. A similar result was obtained in economics by Ellison (2010), who finds that after they have received their tenure, the economists of top US departments slow down their publications pace in top journals.

It is also interesting to note that the East Coast has a significant positive effect over the Midwest (2 standard deviations). The West Coast stands in between.

Finally the effect of public universities is slightly negative but not significant. This could be attributed to higher teaching loads than in private universities. The difference becomes significant when taking into account the endowment per student, which is concentrated almost only on private universities.

The impact of age: variations between countries

It is often believed that the productivity of mathematicians declines rapidly with age. We show here that this is not the case, but that there are important cross-country differences in the life-cycle productivities of mathematicians. These differences might be explained by features such as the ages at which long-term or permanent positions can be obtained, the grant systems, and more generally the nature of the incentives given to scientists, as well as the degree of mobility between institutions, and the variability of teaching loads. The

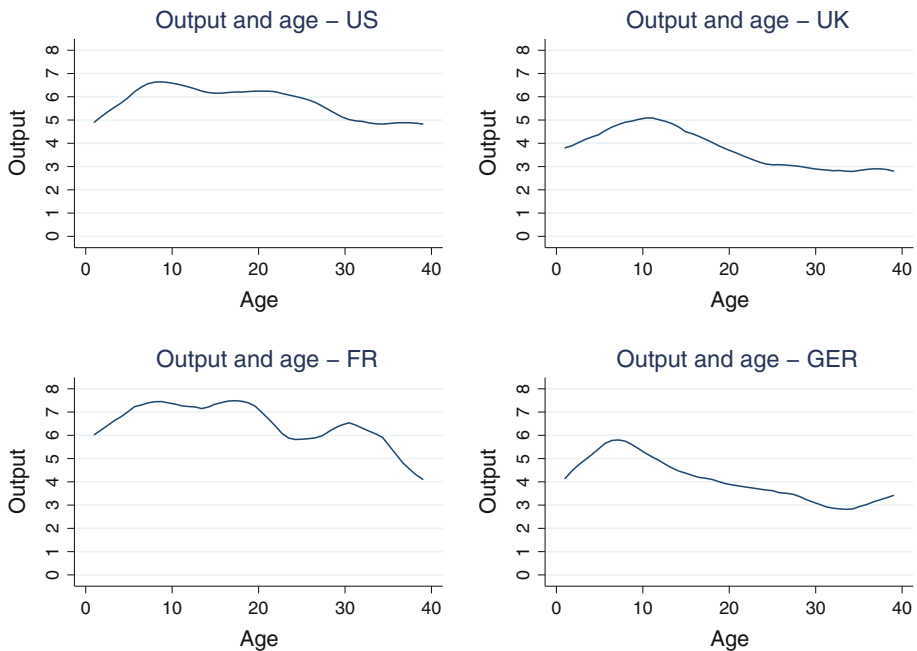


Fig. 1 Variation of productivity with age, selected countries

following figure represents a cross-country comparison of the profiles of scientific productivity of mathematicians as a function of their “age”, defined as the number of years that have elapsed since their first publication.

Figure 1 shows how “age”—the number of years after the first publication – influences the production of mathematicians in different countries. Obviously, there are important differences in the average scientific output of researchers between countries. However the allocation of this output through time also varies strongly between countries. The graphs indicate that some countries are better than other at helping their researchers to remain active. For instance, in Germany, the peak productivity is reached at a younger age than in Britain or the United States, and decrease in production is then steeper. However, the overall picture shows that there is much more variation of productivity across countries than across ages of mathematicians within a country. We can interpret this finding in terms of life cycle evolution of the mathematician’s productivity. However there can also be cohort-effects as found by Oyer (2006). But the length of the time period covered by our data allows us to be confident that the age effects that we have identified are indeed present. A possibility remains that the younger cohorts observed in the 2000s would not behave as their older cohorts during the same period when they will grow older.

Conclusion

The analysis presented here has some interesting implications for individual researchers, departments, or in terms of scientific policy.

Our results shed some light on the possibility for the academic community to detect promising mathematicians from their current production. The main indicator of future success for a young mathematician is obviously the quality of his current publications. However, our results tend to indicate some less obvious criteria, which can be measured over the first few years of activity, and are correlated with a higher future scientific output. Among those, we can cite a wide spectrum of interests. The capability to collaborate with colleagues having different mathematical interests is a good predictor of success. In other words, a strong focus on one area, which is sometimes presented as a way for young scientists to gain a head start, could be counter-productive in the longer term. The total number of collaborations, on the other hand, has more complex implications. Having a large number of past coauthors appears positively correlated to the output, but a large number of current coauthors appears to have a negative impact, probably meaning that increasing co-authorship is inefficient in the short run but has a positive effect in the longer run.

Then, our results also suggest suitable policies or recommendations to improve a mathematics department or mathematical research on a large scale.

For example, encouraging mobility appears to be a way to improve both the quality of a department and the scientific output of its members. On the other hand, encouraging members of a department to collaborate more does not appear to be efficient, except if the collaboration is with colleagues from different areas. This suggests that reading groups or seminars bringing together mathematicians with different specialties could be a way to broaden their interests and to improve their output.

Concentration on some subfields has mixed effects: it appears to lower the output of the department through the hiring of less productive mathematicians, but allows to get better papers from mathematicians with a given talent.

Concerning the global mathematical research, again a high level of mobility seems to have positive effects. By contrast, allocating large subsidies to some departments appears to be useless: it may attract the more active researchers to the richer departments, but does not increase their output when taking into account authors fixed effects.

An important question, for which we do not have a definite answer, is how important it is to train young researchers in the most active departments. One problem here is that it is difficult to distinguish the quality of the training from the intrinsic “talent” of mathematicians.

Finally, an extension of our results to other scientific areas than mathematics would probably be hazardous. There are many differences across sciences: for instance the importance of funding is fundamentally different between experimental fields and the more theoretical ones. It would be interesting to check to what extent our findings for mathematics are also valid in other fields, but this would require the availability of an exhaustive and easy-to-use data set on publications in other fields, comparable to Mathematical Reviews for mathematics.

Appendix 1: additional tables

See Tables [8](#), [9](#), [10](#), [11](#), [12](#),[13](#),[14](#),[15](#),[16](#),[17](#), [18](#), [19](#), [20](#), [21](#), [22](#), [23](#) and [24](#) .

Table 8 Fixed effects of major departments

Variables	(1) Author impact	(2) Author impact	(3) Author impact	(4) Author impact
IAS Princeton	16.05*** (1.782)	-1.061 (4.847)	-1.194 (8.961)	-9.333 (7.363)
Princeton	10.72*** (1.066)	-5.216 (4.333)	-2.509 (8.647)	-7.118 (6.797)
Harvard	8.922*** (1.236)	-0.818 (4.816)	2.318 (9.373)	-17.97** (7.290)
U Paris 11	6.030*** (0.982)	-8.928 (7.109)	5.648 (12.79)	-8.991 (11.05)
NYU	4.576*** (1.031)	7.692 (4.716)	16.00* (8.833)	-9.464 (7.901)
U Chicago	2.713** (1.125)	2.851 (4.724)	1.674 (9.000)	-7.482 (7.220)
MIT	0.510 (0.902)	-3.570 (4.476)	-3.369 (8.806)	-15.93** (6.697)
Columbia	0.296 (1.300)	0.843 (5.730)	-2.620 (10.77)	-13.02 (8.782)
UC Berkeley	-3.498*** (0.836)	-8.892** (4.408)	-10.12 (8.815)	-15.67** (6.976)
U Paris 6	-3.262*** (0.870)	-6.691 (7.158)	0.0252 (12.85)	-8.272 (11.75)
UCLA	-1.423 (1.051)	-0.517 (5.077)	1.788 (9.944)	-8.791 (7.591)
Stanford	-4.031*** (0.997)	-5.427 (4.684)	-2.757 (9.188)	-15.62** (7.171)
U Michigan	-4.579*** (0.961)	-11.04** (4.594)	-17.80* (9.333)	-16.59** (6.919)
Rutgers	-3.688*** (1.001)	-1.294 (5.270)	2.956 (10.12)	-9.720 (8.748)
Purdue	-3.523*** (1.018)	0.862 (5.672)	11.04 (9.342)	-24.68** (10.94)
U Minnesota	-5.918*** (0.942)	-0.841 (4.903)	5.120 (9.166)	-6.019 (7.638)
U Maryland	-4.042*** (1.033)	-3.216 (5.408)	-0.451 (9.438)	-4.440 (10.03)
U Toronto	-4.372*** (1.101)	1.161 (5.793)	5.179 (11.73)	-6.598 (8.163)
Ohio State U	-4.582*** (1.073)	-6.306 (5.446)	-10.32 (10.03)	-8.295 (8.518)
U Wisconsin	-6.897*** (0.994)	0	0	0
Constant	27.26*** (1.758)	28.51*** (6.261)	34.82*** (10.41)	22.46** (9.662)
Author fixed effects	No	Yes	Yes	Yes
R^2		0.417	0.471	0.450
Observations	34,291	34,291	14,868	19,423
Period			<1995	>1994

Table 9 Fixed effects of a selection of major departments, with and without local journals removed

Variables	(1) Author impact	(2) Author impact	(3) Author impact	(4) Author impact	(5) Author impact
Princeton	-1.697 (3.779)	-2.648 (3.694)	-6.465* (3.519)	-3.700 (3.449)	-1.443 (3.793)
U Paris 11	-4.269 (7.844)	-4.370 (7.668)	2.553 (7.304)	-7.670 (7.159)	-5.237 (7.873)
NYU	12.61*** (4.655)	-3.225 (4.551)	12.56*** (4.335)	12.88*** (4.249)	12.60*** (4.672)
IAS Princeton	2.674 (5.145)	1.986 (5.029)	1.025 (4.790)	-3.113 (4.695)	3.282 (5.163)
Constant	31.62*** (7.895)	26.99*** (7.718)	30.93*** (7.352)	31.79*** (7.206)	30.81*** (7.924)
R ²	0.013	0.012	0.013	0.016	0.013
Observations	19,547	19,547	19,547	19,547	19,547
Number of authors	7,373	7,373	7,373	7,373	7,373
Removed	None	CPAM	Annals	IHES	E.N.S.

Table 10 Effect of individual and department variables on authors' impacts and number of articles

Variables	(1) Author impact	(2) Author impact	(3) Nb. articles	(4) Nb. articles
Nb. of coauthors	-4.051*** (0.122)	-4.024*** (0.121)	0.0296*** (0.00255)	0.0291*** (0.00254)
Age	0.551*** (0.0715)	0.573*** (0.0714)	0.0226*** (0.00163)	0.0219*** (0.00165)
Age ²	-0.0245*** (0.00339)	-0.0253*** (0.00333)	-0.000802*** (8.27e-05)	-0.000803*** (8.21e-05)
Age ³	0.000229*** (4.93e-05)	0.000231*** (4.86e-05)	7.65e-06*** (1.26e-06)	7.64e-06*** (1.24e-06)
Univ. specialization index	3.155*** (0.999)	3.075*** (0.945)	3.82e-05 (0.0272)	0.0150 (0.0281)
Size of University	0.0315*** (0.00767)	-0.0278** (0.0140)	0.000724*** (0.000161)	0.00146*** (0.000303)
Stability	2.026 (1.899)	4.855*** (1.733)	0.0480 (0.0421)	0.0551 (0.0446)
Author fixed effects	Yes	Yes	Yes	Yes
Year fixed effects	Yes	Yes	Yes	Yes
Field fixed effects	Yes	Yes	Yes	Yes
University fixed effects	No	Yes	No	Yes
R ²	0.011	0.020	0.005	0.008
Observations	138,707	138,707	138,707	138,707
Number of authors	30,266	30,266	30,266	30,266

Table 11 The determinants of mathematicians' scientific output, without/with fixed effects, US only

Variables	(1) Author impact	(2) Author impact	(3) Author impact
Nb. of coauthors	-5.967*** (0.234)	-4.530*** (0.256)	-4.524*** (0.254)
Age	1.286*** (0.103)	0.513*** (0.143)	0.482*** (0.143)
Age ²	-0.0509*** (0.00502)	-0.0205*** (0.00659)	-0.0203*** (0.00656)
Age ³	0.000514*** (6.71e-05)	0.000141 (9.24e-05)	0.000132 (9.23e-05)
University specialization index	-0.651 (1.891)	4.010 (2.807)	2.043 (2.335)
Size of University	0.0993*** (0.0101)	0.0195 (0.0163)	-0.0321 (0.0282)
Closeness	-26.26*** (3.574)	-3.308 (5.947)	3.965 (4.009)
Private University	4.511*** (0.717)	2.072* (1.128)	
Endowment per Student	4.615*** (1.276)	-2.256 (1.611)	
East coast University	4.081*** (0.619)	1.708 (1.082)	
West coast University	2.784*** (0.858)	0.215 (1.498)	
Author fixed effects	No	Yes	Yes
Year fixed effects	Yes	Yes	Yes
Field fixed effects	Yes	Yes	Yes
University fixed effects	No	No	Yes
R ²	0.127	0.431	0.436
Observations	52,599	52,599	52,599

Table 12 Comparative characteristics of articles in different fields

Field	Authors/paper	Pages/paper	Mean weight	# Authors	# Articles
Algebra	1.98	23.73	31.34	2,463	8,454
Analysis	2.07	19.70	16.46	8,438	31,194
DynSys	2.32	23.61	22.65	1,420	4,798
GeomAlg	1.84	23.36	36.43	4,101	16,720
GeomDiff	1.99	22.69	28.72	5,814	23,544
Numeric	2.30	19.75	10.17	4,638	17,420
PDE	2.10	23.13	21.32	5,898	25,390
Physics	2.47	21.59	12.79	4,455	12,362
ProbaStat	2.13	18.37	8.16	1,0244	41,721
Topology	1.87	25.13	39.09	2,238	9,065

Table 13 Proportions (in %) of international collaborations over time

Years	Country										
	CA	FR	GER	IL	IT	JAP	PRC	RUS	SP	UK	US
1984–1986	62	51	47	57	39	29	65	22	33	48	25
1987–1990	58	50	54	66	40	36	58	25	39	52	26
1991–1994	60	50	54	62	48	31	51	55	36	53	28
1995–1998	58	49	54	61	44	36	49	72	38	54	32
1999–2002	67	47	57	63	46	41	39	76	42	56	37
2003–2006	64	51	58	64	45	48	51	79	43	60	37
Average	62	49	56	63	45	39	48	66	41	55	32

Table 14 Transition matrix of mathematicians: locations of the mathematicians who have started in a given country

Country of first location	Country of current location												Total years
	CA	FR	GER	IL	IT	JAP	OTH	PRC	RUS	SP	UK	US	
CA	66.9	1.8	0.6	1.6	0.2		4.3	0.1		0.9	1.2	22.5	2226
FR	0.6	90.0	1.1	0.2	0.6	0.2	2.3			1.0	0.6	3.4	5403
GER	1.0	1.6	81.4		0.5	0.1	5.2	0.2		0.0	2.7	7.2	5042
IL	3.3	0.8	0.2	68.7			2.3		0.1		2.3	22.2	1204
IT	0.2	2.6	1.0		91.6		2.0			0.3	0.5	1.8	2192
JAP			1.0		0.1	92.7	2.2	0.9			0.2	2.8	2020
OTH	0.8	2.3	2.2	0.1	0.4	0.1	83.9	0.8		0.1	1.3	8.0	12341
PRC	2.6	1.1	0.8	0.1	0.2		3.8	80.5		0.1	0.6	10.2	1914
RUS	2.1	0.6	2.1		1.2		7.0		61.2		9.4	16.4	330
SP		0.7	0.3		0.0		0.9	0.2		96.6	0.4	0.8	2349
UK	2.2	1.7	2.3	0.1	1.1	0.2	11.5	1.5		0.2	68.8	10.3	3618
US	2.2	1.0	0.9	1.0	0.8	0.2	6.8	0.7	0.0	0.5	1.6	84.3	22882
Total years	2455	5701	4848	1173	2384	1971	13326	1930	210	2508	3371	25921	65798

Numbers in columns do not sum to 100, due to imbalance of flows across countries

Table 15 Mean impact of mathematicians depending on country of first location and current country

Country of 1st location	Country of current location												Total
	CA	FR	GER	IL	IT	JAP	OTH	PRC	RUS	SP	UK	US	
CA	4.9	2.2	18.2	8.9	3.2		4.1	0.5		12.0	2.5	6.1	5.3
FR	5.1	12.4	7.8	50.9	14.6	13.9	10.8			19.7	26.5	11.3	12.5
GER	17.1	24.8	8.2		8.0	34.1	9.3	6.1		128.3	11.2	16.2	9.3
IL	11.5	38.4	10.8	8.9			3.3		9.5		41.0	19.5	12.2
IT	18.0	8.5	4.9		5.6		4.5			11.0	2.1	7.1	5.7
JAP			14.8		3.5	10.9	6.2	0.2			17.1	14.5	10.9
OTH	5.8	13.1	8.9	2.7	8.4	6.2	5.1	4.4		16.3	7.4	14.1	6.1

Table 15 continued

Country of 1st location	Country of current location												Total
	CA	FR	GER	IL	IT	JAP	OTH	PRC	RUS	SP	UK	US	
PRC	4.9	30.2	12.2	0.8	9.2		13.2	4.1		22.7	6.9	9.3	5.4
RUS	25.6	8.8	27.2		5.3		13.8		6.3		18.6	48.3	15.7
SP		12.1	1.6		0.8		0.6	31.5		4.7	0.9	9.0	4.7
UK	4.9	17.6	15.5	2.3	5.4	15.8	3.8	3.7		2.0	6.6	12.7	7.2
US	14.2	21.9	18.7	9.7	14.4	7.0	8.3	13.2	8.3	6.0	11.9	8.9	9.3
Total	7.7	13.1	8.9	9.3	6.6	10.9	5.7	5.1	6.4	5.3	8.1	9.4	8.5

Table 16 Number of “permanent” moves from one country to another

From	To												Total
	CA	FR	GER	IL	IT	JAP	OTH	PRC	RUS	SP	UK	US	
CA	0	9	5	5	3	1	38	10	1	2	16	140	230
FR	10	0	12	7	16	2	40	6	1	12	12	62	180
GER	13	37	0	2	10	13	115	5	3	1	48	114	361
IL	7	6	2	0	0	0	6	0	0	0	0	73	94
IT	3	10	5	0	0	0	19	2	0	1	6	26	72
JAP	0	2	12	0	1	0	7	5	0	0	1	18	46
OTH	35	82	100	3	18	9	0	53	8	8	65	315	696
PRC	12	5	4	0	5	2	34	0	0	0	12	43	117
RUS	2	12	14	6	5	0	28	0	0	2	17	49	135
SP	0	2	3	0	1	0	10	0	2	0	5	6	29
UK	12	18	13	1	7	1	67	14	2	3	0	91	229
US	114	65	90	88	40	23	319	42	7	17	85	0	890
Total	208	248	260	112	106	51	683	137	24	46	267	937	3,079

Table 17 Mean impact over lifetime of mathematicians moving from one country to another

From	To										
	CA	FR	GER	IL	IT	JAP	PRC	RUS	SP	UK	US
CA	4.9	9.6	6.5	2.6	12.4	21.3	4.6	4.2	3.2	6.3	9.1
FR	9.3	12.4	20.8	22.4	7.9	8.4	12.5	1.5	28.5	16.1	25.5
GER	23.3	15.4	8.2	13.0	9.2	17.5	5.3	3.7	4.8	12.0	16.7
IL	11.6	5.6	7.8	8.9							19.0
IT	4.7	9.9	13.1		5.6		11.6		1.7	10.6	14.5
JAP		2.4	10.6		16.6	10.9	9.3			8.3	26.8
PRC	4.2	21.2	9.6		8.4	0.6	13.2			3.2	9.3
RUS	0.6	14.3	10.0	3.2	3.3			6.3	21.3	9.1	19.1
SP		7.9	14.2		2.5			21.3	4.7	15.0	4.1
UK	9.0	12.7	15.6	40.9	12.2	21.3	11.1	1.7	7.4	6.6	15.9
US	14.2	26.9	18.8	15.7	17.4	9.4	16.1	9.7	11.3	15.0	8.9

Table 18 Size and share of top authors in top departments

University	Rank	Size	Share 1st author	Share 5 authors	Share 10 authors
Princeton	1	96.9	5.9	19.5	30.3
Paris 11 (F)	2	105.5	11.8	25.1	36.2
MIT	3	123.2	11	24.1	34.2
NYU	4	102.5	6.2	19.8	29.1
Berkeley	5	146	4.1	14.6	23.4
Harvard	6	64.9	10	29.9	41.4
Paris 6 (F)	7	143.1	13.5	22	28.5
Chicago	8	81.1	7	21.4	31.8
UCLA	9	93.8	7.6	26.9	36.2
Stanford	10	106.7	6.1	21	34.3
Michigan	11	111.8	4.6	15.7	24.9
Rutgers	12	104.2	6	22.2	33.2
Purdue	13	95.5	5.9	22.6	35.9
Minnesota	14	116.5	5.4	18.3	30.3
Maryland	15	95.6	8.3	28.5	42.4
IAS Princeton	16	33.2	12	30.9	41
Toronto	17	78.7	14.5	29.8	42.2
Ohio State	18	86	7	19.5	33.1
Columbia	19	57.2	8.9	26.9	42.4
Wisconsin	20	101.3	5.9	20.4	33.5
Cornell	21	106.5	5.6	22.9	35.2
Oxford (UK)	22	80.6	8.5	28.9	40.5
Paris 7 (F)	23	49.5	6.4	23.8	38.2
Caltech	24	54.2	10	31.5	44.8
SUNY Stony Brook	25	46.1	12.2	42.6	61.3
Polytechnique (F)	26	56	7.6	19	31.3
UC San Diego	27	69.9	5.2	19.7	33.9
Hebrew U (IL)	28	64.3	10.2	35.9	51
Cambridge (UK)	29	79.8	6.2	20.7	31.8
Illinois at Urbana	30	99.2	4.4	17.4	28.3

Table 19 Fixed effects of major departments, by IF

Variables	(1) Author impact (IF)	(2) Author impact (IF)	(3) Author impact (IF)	(4) Author impact (IF)
Princeton	13.67*** (0.670)	7.531 (7.304)	3.684 (13.62)	20.07 (13.56)
U Paris 11	5.701*** (0.650)	13.92* (7.871)	4.931 (15.58)	26.36* (13.72)
MIT	6.617*** (0.576)	4.792 (7.350)	2.249 (13.63)	11.01 (13.49)
NYU	15.84*** (0.660)	18.93*** (7.289)	19.61 (13.51)	23.61* (13.64)
UC Berkeley	5.397*** (0.550)	3.025 (7.395)	-3.340 (13.73)	12.28 (13.67)

Table 19 continued

Variables	(1) Author impact (IF)	(2) Author impact (IF)	(3) Author impact (IF)	(4) Author impact (IF)
U Paris 6	3.412*** (0.581)	7.427 (7.975)	-16.64 (15.79)	26.11* (13.82)
U Chicago	5.509*** (0.722)	12.08 (7.604)	10.62 (14.36)	19.11 (13.75)
UCLA	2.864*** (0.698)	9.197 (7.539)	9.018 (13.70)	23.63* (13.98)
Stanford	6.347*** (0.632)	4.958 (7.469)	7.026 (14.28)	9.300 (13.76)
U Michigan	-0.628 (0.629)	0.414 (7.541)	-13.17 (14.24)	10.21 (13.82)
Rutgers	-0.0867 (0.669)	7.690 (7.661)	13.03 (13.86)	17.53 (14.58)
U Maryland	-0.0430 (0.703)	1.027 (7.858)	9.034 (14.34)	1.723 (15.27)
IAS Princeton	-4.898*** (1.099)	9.959 (7.602)	13.38 (14.17)	14.91 (13.77)
Cornell	0.633 (0.652)	3.751 (7.647)	6.776 (13.94)	10.52 (14.23)
Oxford	-3.465*** (0.731)	2.533 (8.310)	8.221 (16.62)	10.56 (14.55)
SUNY Stony Brook	-6.415*** (0.998)	9.447 (8.510)	12.18 (14.84)	11.78 (17.14)
Ecole polytechnique	-4.857*** (0.884)	7.034 (8.061)	-3.952 (16.21)	16.54 (14.12)
Hebrew U	-5.928*** (0.873)	2.925 (8.092)	7.736 (14.97)	-9.118 (14.61)
Cambridge	-2.631*** (0.726)	8.007 (8.262)	19.05 (16.39)	15.30 (14.45)
U Illinois	-4.731*** (0.668)	6.318 (8.179)	8.410 (15.92)	9.860 (14.33)
U Toulouse 3	-8.895*** (0.900)	9.199 (9.021)	19.88 (19.91)	20.90 (14.83)
ENS Paris	-6.966*** (1.011)	8.520 (8.106)	-13.18 (16.60)	21.69 (13.74)
ETH Zürich	-4.842*** (0.864)	1.472 (6.808)	12.70 (10.99)	8.289 (13.62)
Tel Aviv U	-4.911*** (0.732)	4.277 (7.952)	8.840 (15.18)	9.269 (14.16)
U Bonn	-6.695*** (0.884)	0 (0)	0 (0)	0 (0)
Constant	13.34*** (0.797)	25.31*** (8.240)	25.22* (14.78)	15.01 (14.54)
Author fixed effects	No	Yes	Yes	Yes
R^2		0.040	0.046	0.045
Observations	208683	21597	8913	12684
Number of authors		8159	4064	5613
Period			<1995	>1994

Table 20 Fixed effects of a selection of major departments, with some journals removed, by IF

Variables	(1) Author impact (IF)	(2) Author impact (IF)	(3) Author impact (IF)	(4) Author impact (IF)	(5) Author impact (IF)
Princeton	7.531 (7.304)	1.605 (6.864)	5.832 (6.665)	9.125 (7.306)	8.075 (7.315)
U Paris 11	13.92* (7.871)	11.90 (7.397)	15.13** (7.182)	12.76 (7.874)	14.07* (7.883)
NYU	18.93*** (7.289)	-1.008 (6.850)	21.42*** (6.651)	20.05*** (7.291)	19.33*** (7.300)
IAS Princeton	9.959 (7.602)	4.070 (7.143)	11.61* (6.936)	10.28 (7.604)	10.73 (7.613)
Ecole polytechnique	7.034 (8.061)	3.685 (7.575)	8.475 (7.355)	6.849 (8.063)	6.047 (8.072)
ENS Paris	8.520 (8.106)	9.214 (7.617)	9.873 (7.396)	8.782 (8.108)	9.009 (8.117)
Constant	25.31*** (8.240)	25.03*** (7.743)	22.06*** (7.519)	24.63*** (8.243)	24.21*** (8.252)
R^2	0.040	0.040	0.043	0.039	0.039
Observations	21597	21597	21597	21597	21597
Number of authors	8159	8159	8159	8159	8159
Removed	None	CPAM	Annals	IHES	E.N.S.

Table 21 Impact, effect of various variables, based on IF

Dependent variable	(1) Author impact	(2) Author impact	(3) Nb. articles	(4) Nb. articles
Coaut	-6.462*** (0.0906)	-5.945*** (0.0842)	0.0314*** (0.00275)	0.0294*** (0.00255)
Age	0.762*** (0.0408)	0.493*** (0.0508)	0.0306*** (0.00156)	0.0228*** (0.00163)
Age ²	-0.0330*** (0.00207)	-0.0201*** (0.00240)	-0.00123*** (9.08e-05)	-0.000868*** (8.27e-05)
Age ³	0.000356*** (2.90e-05)	0.000175*** (3.55e-05)	1.32e-05*** (1.41e-06)	8.37e-06*** (1.26e-06)
University specialization Index_univ	-4.301*** (0.585)	3.607*** (0.741)	-0.0419* (0.0227)	0.110*** (0.0273)
Size University	0.106*** (0.00378)	0.0416*** (0.00410)	0.00260*** (0.000139)	0.00201*** (0.000133)
Stability	-7.395*** (0.860)	1.232 (1.234)	0.0148 (0.0349)	0.0244 (0.0422)
Constant	18.84*** (1.098)	24.76*** (1.232)	0.950*** (0.0340)	1.200*** (0.0445)
Author fixed effects	No	Yes	No	Yes
Year fixed effects	Yes	Yes	Yes	Yes
Field fixed effects	Yes	Yes	Yes	Yes
R^2	0.093	0.041	0.028	0.008
Observations	138,707	138,707	138,707	138,707
Number of authors		30,266		30,266

Table 22 The determinants of mathematicians' scientific output, without/with fixed effects, US only

Variables	(1) Author impact	(2) Author impact
Nb. of coauthors	-8.131*** (0.221)	-7.432*** (0.218)
Age	1.359*** (0.0926)	0.642*** (0.124)
Age ²	-0.0540*** (0.00444)	-0.0250*** (0.00567)
Age ³	0.000546*** (5.83e-05)	0.000179** (7.80e-05)
University specialization index	4.850 (5.942)	5.805 (6.119)
Size of University	0.0738*** (0.00663)	0.0621*** (0.0102)
Closeness	-27.76*** (5.010)	-3.871 (7.232)
Private University	3.176*** (0.511)	1.824** (0.838)
Endowment per student	3.207*** (0.883)	-1.419 (1.043)
East coast University	2.301*** (0.469)	2.261*** (0.869)
West coast University	1.711*** (0.608)	0.839 (1.053)
Constant	35.78*** (5.975)	32.59*** (6.637)
Author fixed effects	No	Yes
Year fixed effects	Yes	Yes
Field fixed effects	Yes	Yes
R ²	0.092	0.041
Observations	37,320	37,320
Number of authors		9,121

Table 23 Effect of individual variables on mathematician's output, by IF

Dependent variable	(1) Author impact	(2) Author impact	(3) Author impact
Nb. of coauthors	-4.737*** (0.0759)	-5.125*** (0.104)	-4.749*** (0.0758)
Nb. coauthors diff specialty	2.161*** (0.220)	3.506*** (0.239)	2.120*** (0.220)
Nb. past moves	1.290*** (0.126)	0.878*** (0.165)	1.461*** (0.126)
pdisc	0.754*** (0.183)	0.0884 (0.278)	0.815*** (0.183)
Nb. of past MSC codes	0.695*** (0.157)	0.783*** (0.232)	0.777*** (0.157)
Nb. of past coauthors	0.997*** (0.0815)	0.483*** (0.0792)	1.019*** (0.0812)

Table 23 continued

Dependent variable	(1) Author impact	(2) Author impact	(3) Author impact
Constant	14.10*** (0.592)	17.38*** (1.194)	17.81*** (0.740)
Author fixed effect	No	Yes	No
Year fixed effects	Yes	Yes	Yes
Field fixed effects	Yes	Yes	Yes
3 Year cohort effects	No	No	Yes
R^2	0.134	0.049	0.137
Observations	108,447	108,447	108,447
Number of authors		44,875	

Table 24 Journals in the database, A–Z

Journal	Mean				
	Total pages	Nb. articles	M.C.Q.	Pages	Nb. authors
ACHA	15,953	819	0.83	19.48	2.50
ACMMS	12,581	756	0.49	16.64	2.5
Acta	23,678	585	2.14	40.48	2.09
AdvApplProba	43,739	2,360	0.36	18.53	2.07
AdvCompMath	20,798	961	0.63	21.64	2.35
Advances	94,806	2,711	1.04	34.97	2.06
AJM	48,824	1,691	1.03	28.87	1.89
AnnApplProba	45,783	1,790	0.81	25.58	2.22
AnnProba	79,936	3,396	0.89	23.54	1.99
AnnStat	87,197	4,140	0.75	21.06	2.03
Annals	63,255	1,605	1.98	39.41	1.98
Arkiv	12,884	710	0.64	18.15	1.79
ASENS	27,757	846	1.19	32.81	1.78
BAMS	13,372	1,044	2.03	12.81	1.97
Bernoulli	19,542	915	0.40	21.36	2.23
Biometrika	36,867	3,622	0.38	10.18	2.16
CMH	26,054	1,285	0.92	20.28	1.90
CombProbaComput	16,808	1,127	0.34	14.91	2.31
Combinatorica	23,545	1,654	0.44	14.24	2.31
CommPDE	69,948	2,495	0.94	28.04	1.90
Compositio	52,333	2,233	0.76	23.44	1.76
ComputComp	10,917	470	0.33	23.23	2.84
Constr	22,313	1,115	0.71	20.01	2.12
CPAM	59,562	1,844	1.67	32.30	2.18
Crelle	89,626	3,568	0.91	25.12	1.85
DCDS	34,491	2,249	0.40	15.34	2.21
DCG	38,155	2,291	0.50	16.65	2.44
Duke	91,063	3,093	1.38	29.44	1.93

Table 24 continued

Journal	Mean				
	Total pages	Nb. articles	M.C.Q.	Pages	Nb. authors
DynSys	4,707	232	0.33	20.29	2.31
Econometrica	42,090	1,832	0.70	22.97	2.04
ElecJComb	22,490	1,613	0.44	13.94	2.20
ElectrCommunProba	3,201	331	0.63	9.67	2.03
ElectronJProba	14,833	500	0.55	29.67	2.25
Expo	12,656	674	0.44	18.78	1.68
FinancStoch	8,686	419	0.78	20.73	2.29
GAFA	29,987	960	1.17	31.24	1.97
GeoTopo	16,950	461	1.28	36.77	1.95
IHES	16,881	330	2.71	51.15	2.02
IhpProba	26,998	1,145	0.69	23.58	2.01
IhpAN	29,750	1,130	1.26	26.33	2.10
IMAJNA	27,521	1,401	0.63	19.64	2.17
Indiana	54,789	2,254	0.91	24.31	2.02
InfinDimAnal	10,403	561	0.62	18.54	2.15
Inventiones	93,613	3,220	1.94	29.07	1.87
Inverse	54,049	3,569	0.81	15.14	2.42
Irmn	41,359	1,978	0.95	20.91	1.95
JAmStatAssoc	44,051	4,339	0.47	10.15	2.37
JCombThA	49,950	3,414	0.54	14.63	2.11
JCombThB	38,601	2,501	0.63	15.43	2.26
JGeomPhys	45,937	2,209	0.38	20.80	2.19
JRStatSocB	17,309	947	0.59	18.28	2.52
JStatPlan	95,233	6,402	0.28	14.88	2.18
JTheorProba	28,841	1,392	0.38	20.72	1.95
JAG	17,880	655	0.78	27.30	1.83
JAMS	34,388	1,000	2.54	34.39	2.11
JCryptol	10,009	475	0.36	21.07	2.56
JDE	14,9292	5,822	0.91	25.64	2.03
JDG	52,365	1,632	1.19	32.09	1.82
JEMS	6,895	230	1.42	29.98	2.25
JFA	161,178	5,732	0.97	28.12	2.08
JLMS	5,0910	3,667	0.65	13.88	1.94
JMAA	268,584	17,941	0.47	14.97	2.05
JMPA	36,215	1,255	1.03	28.86	2.18
JNLS	18,661	637	0.75	29.30	2.44
MAMS	107,327	984	1.58	109.07	2.11
MathAnn	82,398	4,237	0.96	19.45	1.81
MathComput	69,607	4,263	0.68	16.33	2.12
MathProg	72,525	3,659	0.65	19.82	2.32
MathZ	75,035	4,401	0.62	17.05	1.80

Table 24 continued

Journal	Mean				
	Total pages	Nb. articles	M.C.Q.	Pages	Nb. authors
MRL	18,007	1,503	0.75	11.98	1.98
Nonlinearity	62,933	3,168	0.55	19.87	2.33
NumLinAlgA	17,725	1,000	0.39	17.73	2.49
NumerMath	77,775	3,603	0.75	21.59	2.20
PTRF	64,525	2,709	0.92	23.82	1.94
PhysicaD	130,332	7,418	0.33	17.57	2.64
PLMS	53,111	1,892	0.99	28.07	2.01
PublMath	15,861	906	0.41	17.51	1.83
QJM	18,410	1,319	0.54	13.96	1.91
Random	27,551	1,343	0.57	20.51	2.38
RMIbero	23,016	771	0.71	29.85	2.04
ScandJStat	20,070	1,327	0.29	15.12	2.10
SiamCO	80,559	3,795	0.71	21.23	2.14
SiamJAM	89,115	4,291	0.49	20.77	2.41
SiamJC	80,871	4,130	0.40	19.58	2.71
SiamJMAA	44,987	2,737	0.67	16.44	2.33
SiamJSC	65,780	3,299	0.61	19.94	2.57
SiamMA	69,467	3,636	0.91	19.11	2.08
SiamNA	93,630	4,513	0.79	20.75	2.27
SiamOpti	38,298	1,897	1.08	20.19	2.42
SiamRev	22,594	1,008	1.01	22.41	2.18
SochProcAppl	61,820	3,320	0.57	18.62	1.98
StatSci	11,825	605	0.23	19.55	2.13
StatSinica	29,945	1,711	0.23	17.50	2.33
StudAM	31,616	1,287	0.31	24.57	2.22
TAMS	187,528	8,770	0.83	21.38	1.93
Topology	34,157	1,732	0.82	19.72	1.85
Total	85,963	4,584	0.74	20.83	2.13

Appendix 2: results based on the *Impact factor*

The data presented in this section are similar to those obtained in other parts of the paper. However, the basic indicators are based on the *IF* rather than on *MCQ*. More precisely, the weight attributed to each article is equal to the number of its pages times the *IF* of the journal where it is published, rather than the square of the *MCQ*.

Table 19 is the analog of Table 8.

Similarly, we have the analog of Table 9 in Table 20 with the impact of authors based on the *IF*.

We now consider the factors playing a part in a mathematician's scientific productivity. Table 21 is the analog of Table 10 based on the *IF* rather than the *MCQ*.

The analog of Table 11 with the impact of authors based on the *IF* is in Table 22 . Finally, Table 23 is the analog of Table 7 based on the *IF*.

Appendix 3: more on the data

Table 24 contain the list of journals used here. With each journal we list the total number of pages published in the sample period, the number of articles, the 2007 *M.C.Q.*, the mean number of pages by article, and the mean number of authors by article. The code used for each journal (in the first column) should make it easy, for those who are familiar with the mathematical literature, to identify each journal.

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